## **Displacement, Distance and the Addition of Vectors**

In grade 10 science we must add vectors graphically – with a scale diagram. Algebraic addition cannot be used, although you may use it to check your answers – next year (gr.11 physics) we will add vectors algebraically with trigonometry.

Vectors having different directions can be added using a graphical method called the **tip to tail** method:

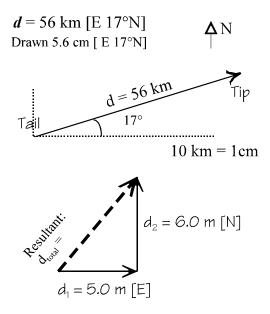
- Draw one vector (to scale) we'll call this the first vector. Be sure to include a label with magnitude if possible.
- At the **tip** of the first vector, determine the direction of the second vector.
- Draw the second vector, using the same scale as the first, with the **tail** of the second at the **tip** of the first vector.
- Draw a line from the **tail** of the first (starting point) to the **tip** of the second (ending point). This new vector represents the sum or **resultant** of the two vectors.
- Measure the **magnitude** and **direction** of the resultant.
- Vectors can be added in any order. Do the vector addition in question #3 two different ways to verify this.

## **Practice Questions:**

- 7. A bear went searching for honey and walks due east for 6.0 km and then 4.0 km due west. Calculate the total distance and resultant displacement.
- 8. Find the displacement of an airplane that flies 5.0 km due east and then turns and flies 7.0 km due north.
- 9. In a bike race, Sebastian pedalled 35 km [E] followed by 40 km [S]. Calculate the total distance travelled, his resultant displacement, and final position.
- 10. Sourdough Sadie left her cabin to look for gold. She walked 8.0 km [S], then 12 km [E], and finally 3.0 km [N]. Calculate Sadie's displacement.
- 11. Sue left home and jogged 3.0 km [S], then 4.0 km [W], and finally 5 km [N 37° E]. Draw a vector diagram to determine Sue's total displacement.
- 12. Explain why you get the same resultant displacement if two displacements are added in the reverse order.

## Note:

**Collinear** vectors are vectors which are along the same straight line (ie parallel or anti-parallel) as in question #1. Collinear vectors can be added without a vector diagram since 4 km [W] = -4 km [E]. Now add the collinear vectors as you would normal integers.



## **Vectors and Directions**

*There are several different conventions for writing directions.* Complete the following directions and diagrams.

| Diagram    | Compass<br>Direction      | Nelson Science<br>textbook method | Bearing<br>(navigation) | RCS direction<br>(math)                    |
|------------|---------------------------|-----------------------------------|-------------------------|--|
|            | [E 40° N]                 | [40° N of E]                      | bearing of 050          | 40° RCS                                    |
| 40°        | or<br>[N 50° E]<br>(why?) | or<br>[50° E of N]                | (clockwise from north)  | (counter-<br>clockwise from<br>+ve x-axis) |
|            |                           |                                   |                         |  |
| 30°        |                           |                                   |                         |  |
|            |                           |                                   |                         |  |
| <u>30°</u> |                           |                                   |                         |  |
| 40°        |                           |                                   |                         |  |
|            | [W 20° S]<br>or           |                                   |                         |  |
|            |                           | [30° W of S]<br>or                |                         |  |
|            | [N]                       |                                   |                         |  |
|            | [W]                       |                                   |                         |  |
|            | [SW]                      |                                   |                         |  |